

MARK SCHEME for the May/June 2014 series

0459 ADDITIONAL MATHEMATICS (US)

0459/02

Paper 2, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes should be read in conjunction with the question paper and the Principal Examiner Report for Teachers.

Cambridge will not enter into discussions about these mark schemes.

Cambridge is publishing the mark schemes for the May/June 2014 series for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level components and some Ordinary Level components.

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<p>1 (i)</p> <p>(ii)</p>	<p>$f(3) = 4$</p> <p>$c = 4$</p> <p>$x^3 - 2x^2 - x - 2 = (x - 3)(x^2 + ax + b) + 4$</p> <p>consts: $-2 = -3b + 4$ $b = 2$ coeffs of x: $-1 = -3a + b$ $a = 1$ coeffs of x^2: $-2 = -3 + a$, $a = 1$ attempt to equate coeffs for one case either $b = 2$ or $a = 1$</p> <p>$(x - 3)(x^2 + x + 2) + 4$</p>	<p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>A1</p>	<p>OR $\begin{array}{r} x^2 + x + 2 \\ x - 3 \overline{) x^3 - 2x^2 - x - 2} \\ \underline{x^3 - 3x^2} \\ x^2 - x \\ \underline{x^2 - 3x} \\ 2x - 2 \\ \underline{2x - 6} \\ 4 \end{array}$</p> <p>M1 for $x^3 - 3x^2$ in working A1 for $x^2 + x \dots$ B1 for remainder of 4 or $c = 4$ stated A1 for $(x - 3)(x^2 + x + 2) + 4$</p>
<p>2 (i) (a)</p> <p>(b)</p> <p>(c)</p> <p>(ii)</p>	<p>$2a$ Real</p> <p>$(a + 2i)(a - 2i)$</p> <p>$a^2 + 2ai - 2ai - (2i)^2$ oe</p> <p>$a^2 + 4$ Real</p> <p>$4i$ Imaginary</p> <p>$\frac{a + 2i}{a - 2i} \times \frac{a + 2i}{a + 2i}$</p> <p>$= \frac{a^2 + 4ai - 4}{a^2 + 4}$</p> <p>$a^2 = 4$</p> <p>$a = \pm 2$</p>	<p>B1</p> <p>M1</p> <p>A1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	<p>correctly multiplying out brackets</p> <p>condone omission of brackets if recovered</p> <p>ft their fraction, making numerator imaginary</p>

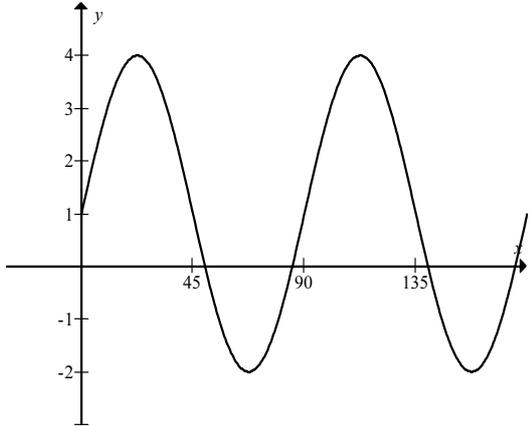
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3	(i)	<p>gradients = $-2, -2, \frac{1}{2}, \frac{1}{2}$</p> <p>Two parallel pairs which are perp.</p>	<p>B1</p> <p>B1</p>	<p>allow second B1 for rearranging equations correctly and commenting even if gradients not explicitly stated</p>
	(ii)	<p>Attempting to solve $2y = x + 3$ and $y = 14 - 2x$</p> <p>or $4y = 2x - 9$ and $y = 4 - 2x$</p> <p>$A(1, 2)$</p> <p>$C(6.5, 1)$</p> <p>$(6.5 - 1)^2 + (1 - 2)^2$ or better</p> <p>$\frac{\sqrt{125}}{2}$ oe or 5.59 (3 sf) cao</p>	<p>M1</p> <p>A1</p> <p>A1</p> <p>M1</p> <p>A1</p>	<p>or Attempting to solve $2y = x + 3$ and $y = 4 - 2x$ or $y = 14 - 2x$ and $4y = 2x - 9$</p> <p>$B(5, 4)$</p> <p>$D(2.5, -1)$</p> <p>$(5 - 2.5)^2 + (4 - -1)^2$ or better</p>
	(iii)	<p>$\left(\frac{1+6.5}{2}, \frac{2+1}{2}\right)$ oe</p> <p>$(3.75, 1.5)$ oe</p>	<p>M1</p> <p>A1</p>	<p>$\left(\frac{5+2.5}{2}, \frac{4-1}{2}\right)$ oe</p> <p>FT</p>
4	(i)	<p>$A^{-1} = B^2$</p> <p>$\Rightarrow AA^{-1} = AB^2$ or $A^{-1}B^{-1} = B^2B^{-1}$</p> <p>$\Rightarrow I = AB^2$ or $A^{-1}B^{-1} = B$</p> <p>$\Rightarrow B^{-1} = AB^2B^{-1}$ or $AA^{-1}B^{-1} = AB$</p> <p>$\Rightarrow B^{-1} = AB$</p>	<p>M1</p> <p>M1</p> <p>A1</p>	<p>attempt left multiplication by A</p> <p>attempt right multiplication by B^{-1}</p>
	(ii)	<p>$\Rightarrow BB^{-1} = BAB$</p> <p>$\Rightarrow I = BAB$</p> <p>$\Rightarrow B^{-1} = BABB^{-1}$</p> <p>$\Rightarrow B^{-1} = BA$</p> <p>$\Rightarrow AB = BA$</p>	<p>M1</p> <p>A1</p>	<p>attempt left multiplication by B or attempt right multiplication by B^{-1}</p> <p>for correct completion</p>
5	(i)	<p>$\frac{5}{6}$ or 0.667 or 0.833 seen</p> <p>$\left(\frac{5}{6}\right)^{25}$</p> <p>= 0.0105 (3 sf)</p>	<p>B1</p> <p>M1</p> <p>A1</p>	<p>allow 1.05%</p>
	(ii)	<p>Small probability oe</p> <p>Probably effective oe</p>	<p>B2,1,0</p>	<p>or very unlikely oe</p> <p>allow "Drug is effective"</p>

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6	(i)	Class <i>A</i> more evenly spread or more widely spread oe Class <i>B</i> has one outlier, <i>A</i> has none oe	B1 B1	or Class <i>B</i> more bunched oe $\frac{4 \times 5 + 5 \times 16 + 6 \times 11 + 7 \times 4 + 8 \times 3}{5 + 16 + 11 + 4 + 3}$
	(ii) (a)	Unchanged oe	B1	
	(b)	Decrease oe	B1	
	(iii) (a)	$\frac{\sum fx}{\sum f}$ attempted $\left(= \frac{218}{39} \right)$ = 5.59 (3 sf)	M1 A1	
	(b)	(With Freda) <i>A</i> better than <i>B</i> but without Freda <i>B</i> better than <i>A</i> oe	B1	
7	(i)	<i>BC</i> = <i>CD</i> (triangle <i>BCD</i> isosceles) <i>CE</i> = <i>CA</i> (angle <i>CAE</i> = angle <i>CEA</i> , base angles of isosceles triangle <i>ACE</i>) <i>BE</i> = <i>DA</i> (given) Triangle <i>BCE</i> is congruent to triangle <i>DCA</i> (SSS) Angle <i>BCE</i> = Angle <i>DCA</i> Therefore <i>BCA</i> + <i>ACE</i> = <i>DCE</i> + <i>ACE</i> <i>BCA</i> = <i>DCE</i> .	B2,1,0 B1	allow B1 for two correct statements with supporting reasons
	(ii) and (iii)	Triangle <i>BCA</i> is congruent to triangle <i>DCE</i> (SAS) Hence <i>AB</i> = <i>ED</i> Angle <i>CBA</i> = Angle <i>CDE</i> Therefore <i>CBD</i> + <i>ABD</i> = <i>CDB</i> + <i>BDE</i> , hence <i>ABD</i> = <i>BDE</i>	B2,1,0 B2,1,0	no need to repeat reasons if given in (i) No need to restate that triangle <i>BCA</i> is congruent to triangle <i>DCE</i> if stated in (ii)

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<p>8 (i)</p> <p>(ii)</p> <p>(iii)</p>	<p>$k = 5$</p> <p>$2\pi R = 5r$ oe</p> <p>$r^2 = R^2 + 10^2$ and a valid attempt to eliminate R</p> <p>Attempt to solve as far as $r =$</p> <p>$r = 16.5$ cao</p> <p>$\frac{1}{2}(\text{their } r)^2 \times 5$ soi</p> <p>awrt 681 or 682</p>	<p>B1</p> <p>M1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	<p>or $\frac{1}{2}r^2(5) = \pi Rr$</p> <p>condone one slip in rearrangement</p>
<p>9 (i)</p> <p>(ii)</p>	<p>$\frac{\sin x}{5} = \frac{\sin 30}{12}$</p> <p>$x = \sin^{-1}\left(\frac{5}{12}\sin 30\right)$ or better</p> <p>132(.02...)</p> <p>$\frac{\text{speed}}{\sin(\text{their } 137.975\dots)} = \frac{12}{\sin 30}$</p> <p>correct</p> <p>time = $\frac{6}{16.06(682\dots)}$</p> <p>0.37 (hours) or 22.4 mins</p>	<p>M1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1</p>	<p>If M0 then SC1 for a correctly orientated and sufficiently labelled sketch</p> <p>or $\frac{\text{distance}}{\sin 30} = \frac{6}{\sin(\text{their } 137.975\dots)}$</p> <p>or $\frac{4.48(128\dots)}{12}$</p>
<p>10 (i)</p> <p>(ii)</p> <p>(iii)</p> <p>(iv)</p>	<p>amplitude 3</p> <p>period 90</p> <p>$f(x) = 1$</p>  <p>0, 45, 90, 135, 180</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B3, 2,</p> <p>1, 0</p> <p>B2</p>	<p>or $y = 1$</p> <p>Correct shape between 0 and 180</p> <p>-2 and 4 marked on vertical axis</p> <p>Passing through at least 2 of (45, 1)</p> <p>(90, 1) and (135, 1)</p> <p>Both maxima and minima correctly located</p> <p>B1 for any 3 correct</p>

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<p>11 (i)</p> <p>(ii)</p> <p>(iii)</p> <p>(iv)</p> <p>(v)</p>	<p>Accuracy of plots</p> <p>Reasonable line of best fit through (3.2, 56) $s = mt + b$ with m between 7 and 11 and b between 22 and 32</p> <p>Every extra 1 hour spent revising gives an increase of <i>their</i> $m\%$ in marks</p> <p>Approx 43%</p> <p>The fact that as the number of hours revising increases, the percentage increases does not mean that the number of hours revising causes the good score. It might be that for example, better students spend more time at their studies than weaker students. oe</p>	<p>B2,1,0</p> <p>B1</p> <p>B1</p> <p>B1FT</p> <p>B1FT</p> <p>B1</p>	<p>–1 each error, allow tolerance ± 1 mm</p> <p>ft their m provided line reasonable</p> <p>or 10 hours is outside the range of this data and it is dangerous to extrapolate beyond the data given oe</p>
<p>12 (a)</p> <p>(b)</p>	<p>Two equations from $17 = 3a + b$ $73 = 17a + b$ $297 = 73a + b$ $a = 4$ $b = 5$</p> <p>$f(0) = 1650$ $f(n+1) = 1.035 \times f(n) \quad n \geq 0$</p>	<p>B1</p> <p>B1</p> <p>B1</p> <p>B2,1,0</p>	<p>correct answers for both a and b imply first B1 if no working seen</p> <p>or $f(1) = 1650$ $f(n+1) = 1.035 \times f(n) \quad n \geq 1$</p>