

Cambridge International AS & A Level

FURTHER MA	ATHEMATICS		9231/3
CENTRE NUMBER		CANDIDATE NUMBER	
CANDIDATE NAME			

Paper 3 Further Mechanics

October/November 2020

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity (g) is needed, use $10 \,\mathrm{m\,s^{-2}}$.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Blank pages are indicated.

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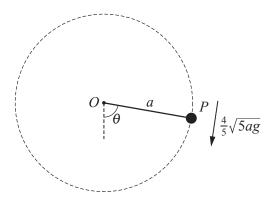


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A particle P of mass m is placed on a fixed smooth plane which is inclined at an angle θ to the horizontal A light spring, of natural length a and modulus of elasticity $3mg$, has one end attached to P and the other end attached to a fixed point O at the top of the plane. The spring lies along a line of greatest slope of the plane. The system is released from rest with the spring at its natural length.				
Find, in terms of a and θ , an expression for the greatest extension of the spring in the subsection.	quent [3]			
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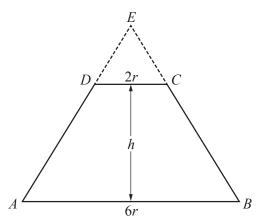
A particle P is attached to one end of a light inextensible string of length a. The other end of the string is attached to a fixed point O. The particle P is held with the string taut and making an angle θ with the downward vertical. The particle P is then projected with speed $\frac{4}{5}\sqrt{5ag}$ perpendicular to the string and just completes a vertical circle (see diagram).

Find the value of $\cos \theta$.	[5]

One end of a light elastic string, of natural length a and modulus of elasticity 4mg, is attached to a

3

(a)	Find the value of k .	[4
(b)	Find the value of $\cos \theta$.	[2
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The diagram shows the cross-section ABCD of a uniform solid object which is formed by removing a cone with cross-section DCE from the top of a larger cone with cross-section ABE. The perpendicular distance between AB and DC is h, the diameter AB is h and the diameter h is h.

)	Find an expression, in terms of h , for the distance of the centre of mass of the solid object from	<i>AB</i> . [4]

The object is freely suspended from the point B and hangs in equilibrium. The angle between AB and the downward vertical through B is θ .

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plan	article P is projected with speed u at an angle α above the horizontal from a point O be and moves freely under gravity. The horizontal and vertical displacements of sequent time t are denoted by x and y respectively.	P from O at
(a)	Derive the equation of the trajectory of P in the form	
	$y = x \tan \alpha - \frac{gx^2}{2u^2} \sec^2 \alpha.$	[
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	point Q is the highest point on the trajectory of P in the case where $\alpha = 45^{\circ}$.	
(b)	Show that the x-coordinate of Q is $\frac{u^2}{2g}$.	



		•••••
(c)	Find the other value of α for which P would pass through the point Q .	[4]
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Two smooth spheres A and B have equal radii and masses m and 2m respectively. Sphere B is at rest on

)	Find, in terms of u and e , the velocities of A and B after the collision.	[3
. (sequently, B collides with a fixed vertical wall which makes an angle θ with the direction where $\tan \theta = \frac{3}{4}$. coefficient of restitution between B and the wall is $\frac{2}{3}$. Immediately after B collideration contains a fixed vertical wall which makes an angle θ with the direction of θ with the direction of θ and the wall is $\frac{2}{3}$. Immediately after B collideration contains a fixed vertical wall which makes an angle θ with the direction of θ with the direction of θ and θ collideration of θ collideration of θ and θ collideration of θ collideration of θ and θ collideration of θ collin	
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Show the	at the velocity vr	ms^{-1} of P is give	en by $v = \frac{100}{100}$	$\frac{1-2x}{x}$.	
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7

Show that x and t are related by the equation x as t becomes large.	(200 1)0	[5

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Additional Page

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