

Cambridge International AS & A Level

FURTHER MA	THEMATICS		9231/3
CENTRE NUMBER		CANDIDATE NUMBER	
CANDIDATE NAME			

Paper 3 Further Mechanics

May/June 2021

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity (g) is needed, use 10 m s⁻².

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has **16** pages. Any blank pages are indicated.

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Find an expression for <i>v</i> i	in terms of t .	

Find x in terms of a .	[6]
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One end of a light elastic string, of natural length a and modulus of elasticity kmg, is attached to a

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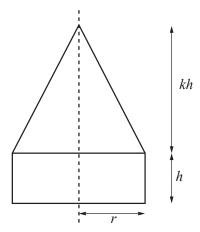
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fixed point A . The other end of the string is attached to a particle P of mass $4m$. The equilibrium a distance x vertically below A .	e particle P hangs in
(a) Show that $k = \frac{4a}{x-a}$.	[1]
An additional particle, of mass $2m$, is now attached to P and the combined particle is at the original equilibrium position of P . When the combined particle has descende speed is $\frac{1}{3}\sqrt{ga}$.	is released from rest ed a distance $\frac{1}{3}a$, its
(b) Find x in terms of a .	[6]

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A uniform solid circular cone has vertical height kh and radius r. A uniform solid cylinder has height h and radius r. The base of the cone is joined to one of the circular faces of the cylinder so that the axes of symmetry of the two solids coincide (see diagram, which shows a cross-section). The cone and the cylinder are made of the same material.

is	$\frac{h(k^2 + 4k + 6)}{4(3+k)}.$
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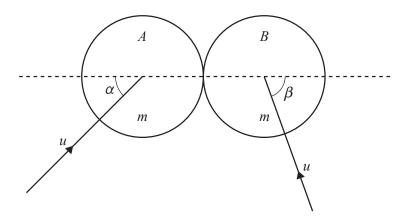
The solid is placed on a plane that is inclined to the horizontal at an angle θ . The base of the cylinder is in contact with the plane. The plane is sufficiently rough to prevent sliding. It is given that 3h = 2r and that the solid is on the point of toppling when $\tan \theta = \frac{4}{3}$.

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5	A particle P of mass m is attached to one end of a light inextensible string of length a . The oth of the string is attached to a fixed point O . The particle completes vertical circles with centre O points O and O are on the path of O , both on the same side of the vertical through O . O makes an O with the downward vertical through O and O makes an angle O with the upward vertical through O and O							
	The speed of P when it is at A is u and the speed of P when it is at B is \sqrt{ag} . The tensions in the string at A and B are T_A and T_B respectively. It is given that $T_A = 7T_B$.							
	Find the value of θ and find an expression for u in terms of a and g . [8]							

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Two uniform smooth spheres A and B of equal radii each have mass m. The two spheres are each moving with speed u on a horizontal surface when they collide. Immediately before the collision, A's direction of motion makes an angle α with the line of centres, and B's direction of motion makes an angle β with the line of centres (see diagram). The coefficient of restitution between the spheres is $\frac{1}{3}$ and $2\cos\beta=\cos\alpha$.

,	it the direction of motion of A after the collision is perpendicular to the line of centr
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The total kinetic energy of the spheres after the collision is $\frac{3}{4}mu^2$. **(b)** Find the value of α . [4]



A particle P is projected from a point O on a horizontal plane and moves freely under gravity. The

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