

Cambridge International AS & A Level

Paper 4 Further	Probability & Statistics		May/June 202
FURTHER MA	ATHEMATICS		9231/43
CENTRE NUMBER		CANDIDATE NUMBER	
CANDIDATE NAME			

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

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[Turn over

1 hour 30 minutes

Farmer A grows apples of a certain variety. Each tree produces 14.8 kg of apples, on average, per year. Farmer B grows apples of the same variety and claims that his apple trees produce a higher mass of apples per year than Farmer A's trees. The masses of apples from Farmer B's trees may be assumed to be normally distributed.

A random sample of 10 trees from Farmer B is chosen. The masses, x kg, of apples produced in a year are summarised as follows.

 $\sum x = 152.0$ $\sum x^2 = 2313.0$

Test, at the 5% significance level, whether Farmer <i>B</i> 's claim is justified.	[6]

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A company is developing a new flavour of chocolate by varying the quantities of the ingredients. A random selection of 9 flavours of chocolate are judged by two tasters who each give marks out of 100 to each flavour of chocolate.

Chocolate	A	В	C	D	Е	F	G	Н	I
Taster 1	72	86	75	92	98	79	87	60	62
Taster 2	84	72	74	95	85	87	82	75	68

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as follows.

The heights, x m, of a random sample of 50 adult males from country A were recorded. The heights, y m,

of a random sample of 40 adult males from country B were also recorded. The results are summarised

	$\Sigma x = 89.0$	$\sum x^2 = 159.4$	$\sum y = 67.2$	$\angle y = 113.1$	
Find a 95% c	onfidence interva	al for the difference	between the mea	an heights of adult male	es from co
A and adult r	nales from countr	ry B.			
•••••					•••••
		•••••			
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of X is given by

X is a discrete random variable which takes the values $0, 2, 4, \ldots$. The probability generating function

Find $E(X)$ and $Var(X)$.	



[Turn over

(a)	Explain how this inform	nation ten	ds to sup	port the	manage	er's susp	oicion.		
		••••••	••••••	••••••	••••••	•	• • • • • • • • • • • • • • • • • • • •	•	
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folloare s	ow a Poisson distribution	. The nui	mbers of	aims that breakage 2	at the nu ges in a	mbers or random	f breaka sample	ges in a of 180	one-hour performance of the following of the following performance of the
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6 The continuous random variable *X* has probability density function f given by

$$f(x) = \begin{cases} \frac{1}{8} & 0 \le x < 1, \\ \frac{1}{28}(8-x) & 1 \le x \le 8, \\ 0 & \text{otherwise.} \end{cases}$$

(a)	Find the cumulative distribution function of X .	[3]
(b)	Find the value of the constant a such that $P(X \le a) = \frac{5}{7}$.	[3]

Γhe	random variable Y is given by $Y = \sqrt[3]{X}$.	
(c)	Find the probability density function of <i>Y</i> .	[5]



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