

Cambridge International AS & A Level

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

721517662

FURTHER MATHEMATICS

9231/32

Paper 3 Further Mechanics

October/November 2021

1 hour 30 minutes

You must answer on the question paper.

You will need: List of formulae (MF19)

INSTRUCTIONS

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.
- Where a numerical value for the acceleration due to gravity (g) is needed, use $10 \,\mathrm{m\,s^{-2}}$.

INFORMATION

- The total mark for this paper is 50.
- The number of marks for each question or part question is shown in brackets [].

This document has 16 pages. Any blank pages are indicated.

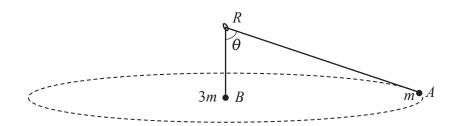
A pa	article is projected with speed u at an angle α above the horizontal from a point O on a horizontal ne. The particle moves freely under gravity.					
(a)	Write down the horizontal and vertical components of the velocity of the particle at time <i>T</i> a projection.					
	time T after projection, the direction of motion of the particle is perpendicular to the direction of ection.					
(b)	Express T in terms of u , g and α . [2]					
(c)	Deduce that $T > \frac{u}{g}$. [1]					

spring. The spring and particle *P* are at rest on the surface.

2

A light spring AB has natural length a and modulus of elasticity 5mg. The end A of the spring is attached to a fixed point on a smooth horizontal surface. A particle P of mass m is attached to the end B of the

Find the value of k .	[6]

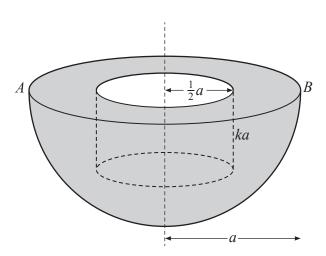


Particles A and B, of masses m and 3m respectively, are connected by a light inextensible string of length a that passes through a fixed smooth ring R. Particle B hangs in equilibrium vertically below the ring. Particle A moves in horizontal circles with speed v. Particles A and B are at the same horizontal level. The angle between AR and BR is θ (see diagram).

(a)	Show that $\cos \theta = \frac{1}{3}$.	[2]
		•••••
(b)	Find an expression for v in terms of a and g .	[4]
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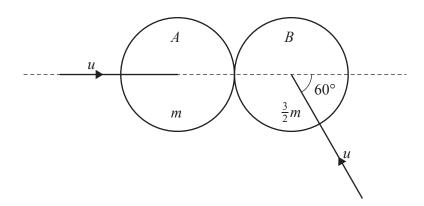
(a)



An object is formed by removing a solid cylinder, of height ka and radius $\frac{1}{2}a$, from a uniform solid hemisphere of radius a. The axes of symmetry of the hemisphere and the cylinder coincide and one circular face of the cylinder coincides with the plane face of the hemisphere. AB is a diameter of the circular face of the hemisphere (see diagram).

Show that the distance of the centre of mass of the object from AB is $\frac{3a(2-k^2)}{2(8-3k)}$.	[4]
	•••••

When the object is freely suspended from the point A, the line AB makes an angle θ with the downward vertical, where $\tan \theta = \frac{7}{18}$.



Two uniform smooth spheres A and B of equal radii have masses m and $\frac{3}{2}m$ respectively. The two spheres are each moving with speed u on a horizontal surface when they collide. Immediately before the collision A's direction of motion is along the line of centres, and B's direction of motion makes an angle of 60° with the line of centres (see diagram). The coefficient of restitution between the spheres is $\frac{2}{3}$.

	Find the angle through which the direction of motion of <i>B</i> is deflected by the collision.
•	

(h)	Find the loss in the total kinetic energy of the system as a result of the collision.	[3]
(D)	I me the loss in the total kinetic energy of the system as a result of the comston.	[2]
		•••••

for	ce of magnitude $\left(8x - \frac{128}{x^3}\right)$ N acts on P in the direction OP. When $t = 0$, $x = 0$	= 8 and v = -15.
) !	Show that $v = -\frac{2}{x}(x^2 - 4)$.	[

t 1	strin aut P be	end of a light inextensible string of length a is attached to a fixed point O . The other end of the a is attached to a particle P of mass a . The particle a is held vertically below a with the string and then projected horizontally. When the string makes an angle of a 0° with the upward vertical, ecomes detached from the string. In its subsequent motion, a 1 passes through the point a 2 which is a since a 3 vertically above a 4.
((a)	The speed of P when it becomes detached from the string is V . Use the equation of the trajectory of a projectile to find V in terms of a and g . [4]

Additional Page

If you use the following lined page to complete the answer(s) to any question(s), the question number(s) must be clearly shown.	

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