

# Cambridge International AS & A Level

CANDIDATE NAME			
CENTRE NUMBER		CANDIDATE NUMBER	
MATHEMATI	cs		9709/3
Paper 3 Pure N	Mathematics 3		May/June 202
			1 hour 50 minute
You must answ	ver on the question paper.		
You will need:	List of formulae (MF19)		

### **INSTRUCTIONS**

- Answer all questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do not use an erasable pen or correction fluid.
- Do not write on any bar codes.
- If additional space is needed, you should use the lined page at the end of this booklet; the question number or numbers must be clearly shown.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.
- Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

#### **INFORMATION**

- The total mark for this paper is 75.
- The number of marks for each question or part question is shown in brackets [ ].

This document has **20** pages. Any blank pages are indicated.

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2 On a sketch of an Argand diagram, shade the region whose points represent complex numbers z satisfying the inequalities  $|z+1-\mathrm{i}| \le 1$  and  $\arg(z-1) \le \frac{3}{4}\pi$ . [4]

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(a)	Explain why the graph of $y$ against $\ln x$ is a straight line and state the exact value of the graph of the line.	dien [3]
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<b>.</b> .		
	s given that the line intersects the y-axis at the point where $y = 1.3$ .  Calculate the value of A, giving your answer correct to 2 decimal places.	[2]
	s given that the line intersects the y-axis at the point where $y = 1.3$ .	[2]
	s given that the line intersects the y-axis at the point where $y = 1.3$ .  Calculate the value of A, giving your answer correct to 2 decimal places.	[2]
	s given that the line intersects the y-axis at the point where $y = 1.3$ .  Calculate the value of $A$ , giving your answer correct to 2 decimal places.	[2]
	s given that the line intersects the y-axis at the point where $y = 1.3$ .  Calculate the value of $A$ , giving your answer correct to 2 decimal places.	[2]
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1	Using integration by parts, find the exact value of $\int_0^2 \tan^{-1}(\frac{1}{2}x) dx$ .	[5]
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Find th exact.	e two squar	e roots of	u, givin	g your a	nswers i	n the for	m <i>a</i> + i <i>b</i>	, where <i>a</i>	and b are re-
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(a)	Prove that $\csc 2\theta - \cot 2\theta \equiv \tan \theta$ .	[3]
(b)	Hence show that $\int_{\frac{1}{4}\pi}^{\frac{1}{3}\pi} (\csc 2\theta - \cot 2\theta) d\theta = \frac{1}{2} \ln 2.$	[4
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A curve is such that the gradient at a general point with coordinates $(x, y)$ is proportional to $\frac{y}{\sqrt{x+1}}$ .				
	The curve passes through the points with coordinates (0, 1) and (3, e).			
	By setting up and solving a differential equation, find the equation of the curve, expressing $y$ in terms of $x$ .			
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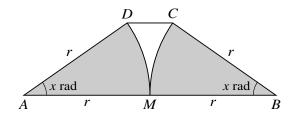
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oordinates of the appropriate.	e stationary points	of the curve.	Give your answ	vers correct to 3 deci	ima] [8]
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9	Let	$f(x) = \frac{14 - 3x + 2x^2}{(2+x)(3+x^2)}.$
	(a)	Express $f(x)$ in partial fractions. [5]

<b>(b)</b>	Hence obtain the expansion of $f(x)$ in ascending powers of $x$ , up to and including the term in $x^2$ [5]



The diagram shows a trapezium ABCD in which AD = BC = r and AB = 2r. The acute angles BAD and ABC are both equal to x radians. Circular arcs of radius r with centres A and B meet at M, the midpoint of AB.

(a)	Given that the sum of the areas of the shaded sectors is 90% of the area of the trapezium, show that $x$ satisfies the equation $x = 0.9(2 - \cos x) \sin x$ . [3]
<b>(b)</b>	Verify by calculation that $x$ lies between 0.5 and 0.7. [2]

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		$x_{n+1} = \cos x$	$s^{-1} \left( 2 - \frac{x}{0.9  s} \right)$	$\frac{n}{\ln x_n}$		
converges,	then it converg	ges to the roo	ot of the equa	ion in part (a).		
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Show that $OA = OB$ and use a scalar product to calculate angle $AOB$ in degrees.

ŀ	Find the possible position vectors of $P$ .	
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